



DEMOCRITOS
DEmocritos MOdeling Center for
Research In aTOMistic Simulation **INFN**



DISORDER AND INTERACTION: GROUND STATE PROPERTIES of the DISORDERED HUBBARD MODEL

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work done in SISSA - Trieste

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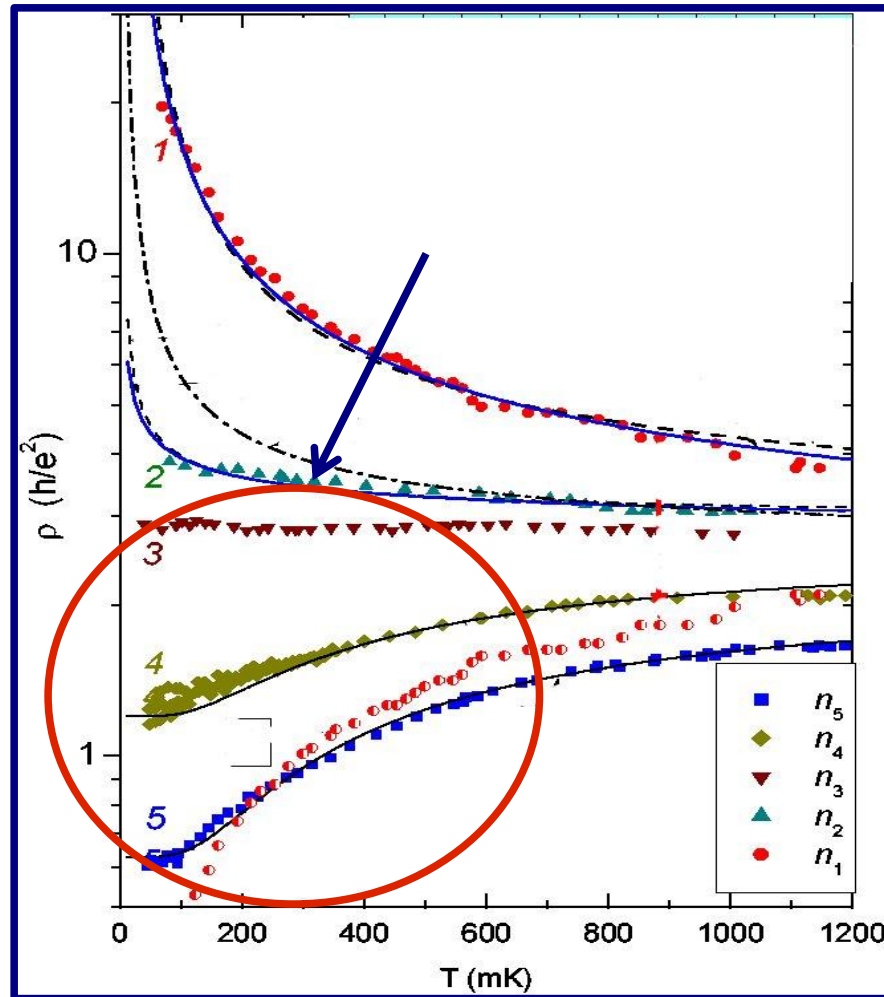
OUTLINE

- AIM: interplay of disorder and interaction
in 2 D Hubbard model
- METHOD: variational wave function within VMC
- RESULTS:
 - transition from Anderson to Mott Insulator
 - paramagnetic and magnetic phase diagram

WHY DISORDER AND INTERACTION ?

METAL-INSULATOR TRANSITION IN 2D

CAN INTERACTION
CREATE AN
EXTENDED STATE IN
2D ?



*Kravchenko et al., Phys. Rev. Lett. **84**, 2909*

*Punnoose et al. Science **310**, 289 (2005)*

ANDERSON LOCALIZATION in COLD ATOMS

COLD ATOMS IN OPTICAL LATTICES ARE A UNIQUE TOOL FOR HIGHLY CONTROLLED INVESTIGATIONS OF MANY BODY SYSTEMS

Direct observation of Anderson localization of matter waves in a controlled disorder

Juliette Billy¹, Vincent Josse¹, Zhanchun Zuo¹, Alain Bernard¹, Ben Hambrecht¹, Pierre Lugan¹, David Clément¹, Laurent Sanchez-Palencia¹, Philippe Bouyer¹ & Alain Aspect¹

Nature, **453**, (2008)
891)

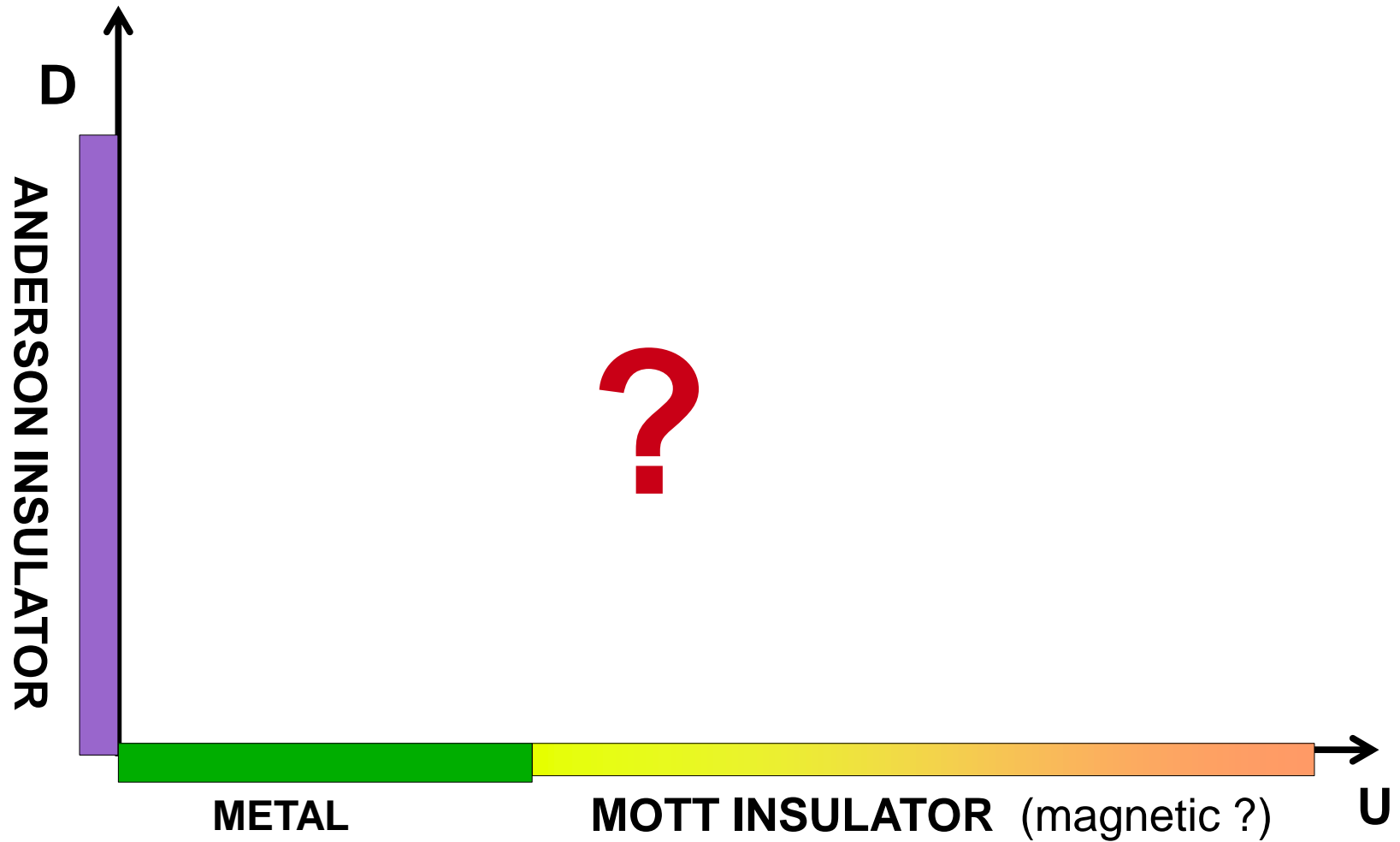
Anderson localization of a non-interacting Bose–Einstein condensate

Giacomo Roati^{1,2}, Chiara D’Errico^{1,2}, Leonardo Fallani^{1,2}, Marco Fattori^{1,2,3}, Chiara Fort^{1,2}, Matteo Zaccanti^{1,2}, Giovanni Modugno^{1,2}, Michele Modugno^{1,4,5} & Massimo Inguscio^{1,2}

Nature, **453**, (2008)
895)

DISORDERED HUBBARD MODEL

2 dimensions half filling

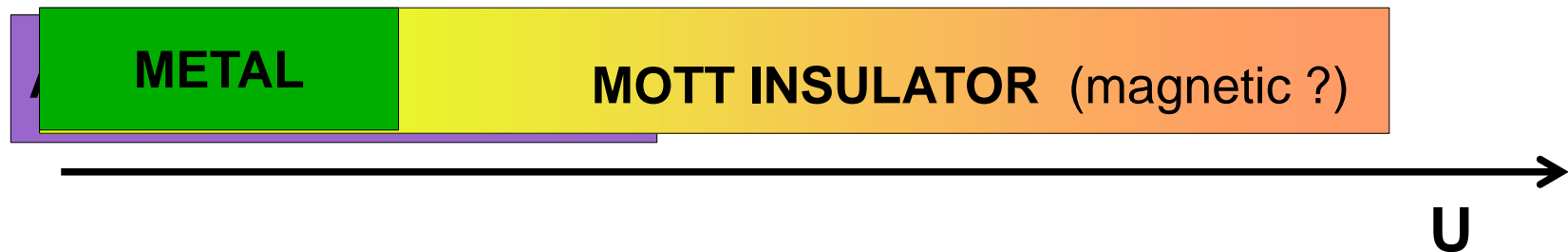


VARIATIONAL WAVE FUNCTION

Disordered wave function with Jastrow correlation

DIAGONALIZE 

$U=0$
 $D \neq 0$

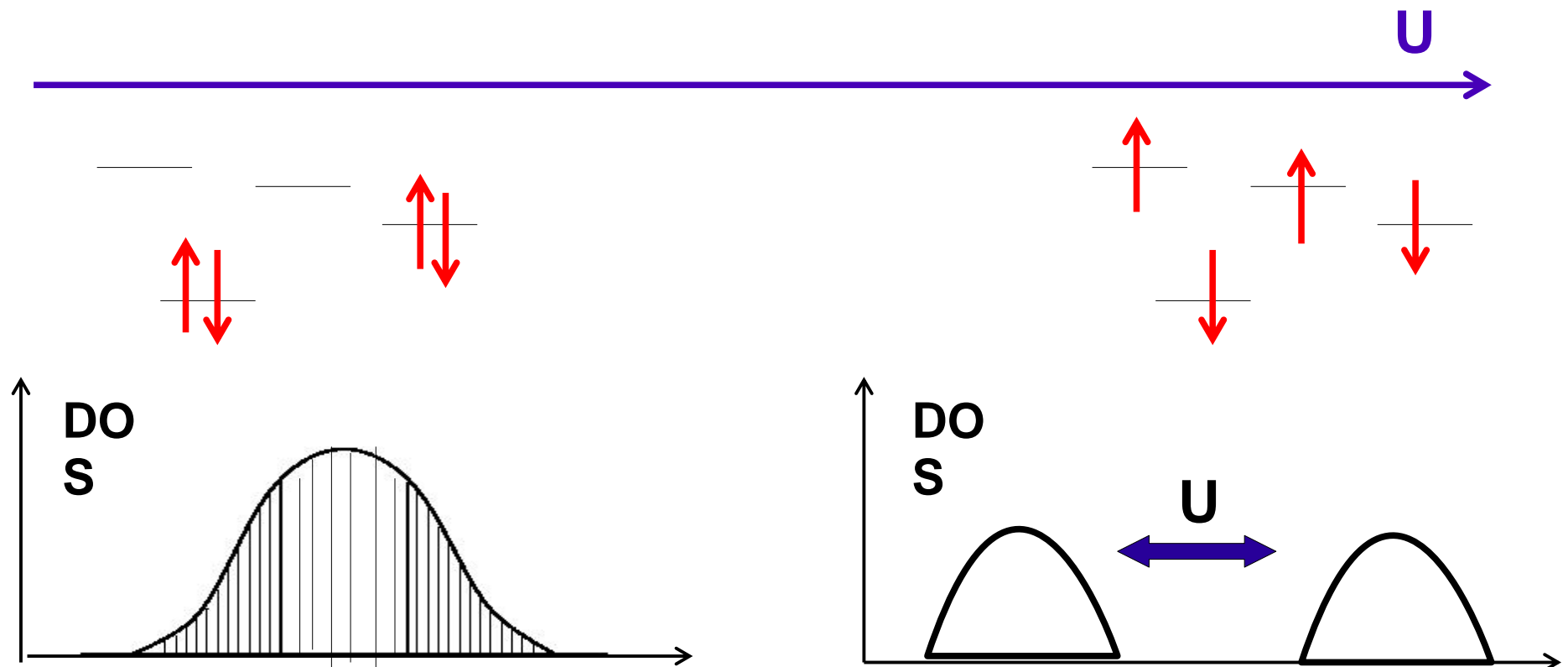


M. Capello, et al. Phys. Rev. Lett **94**, 026406 (2005) 7

ENERGY COMPETITION

**ANDERSON
INSULATOR**

**MOTT
INSULATOR**



*HOW CAN WE DISTINGUISH BETWEEN A MOTT
AND AN ANDERSON INSULATOR ?*

**The properties of excitations of a system are
reflected in a different arrangement
of the electrons in the ground state**

Kohn, Phys. Rev. 133, A171 (1964)

Static structure factor

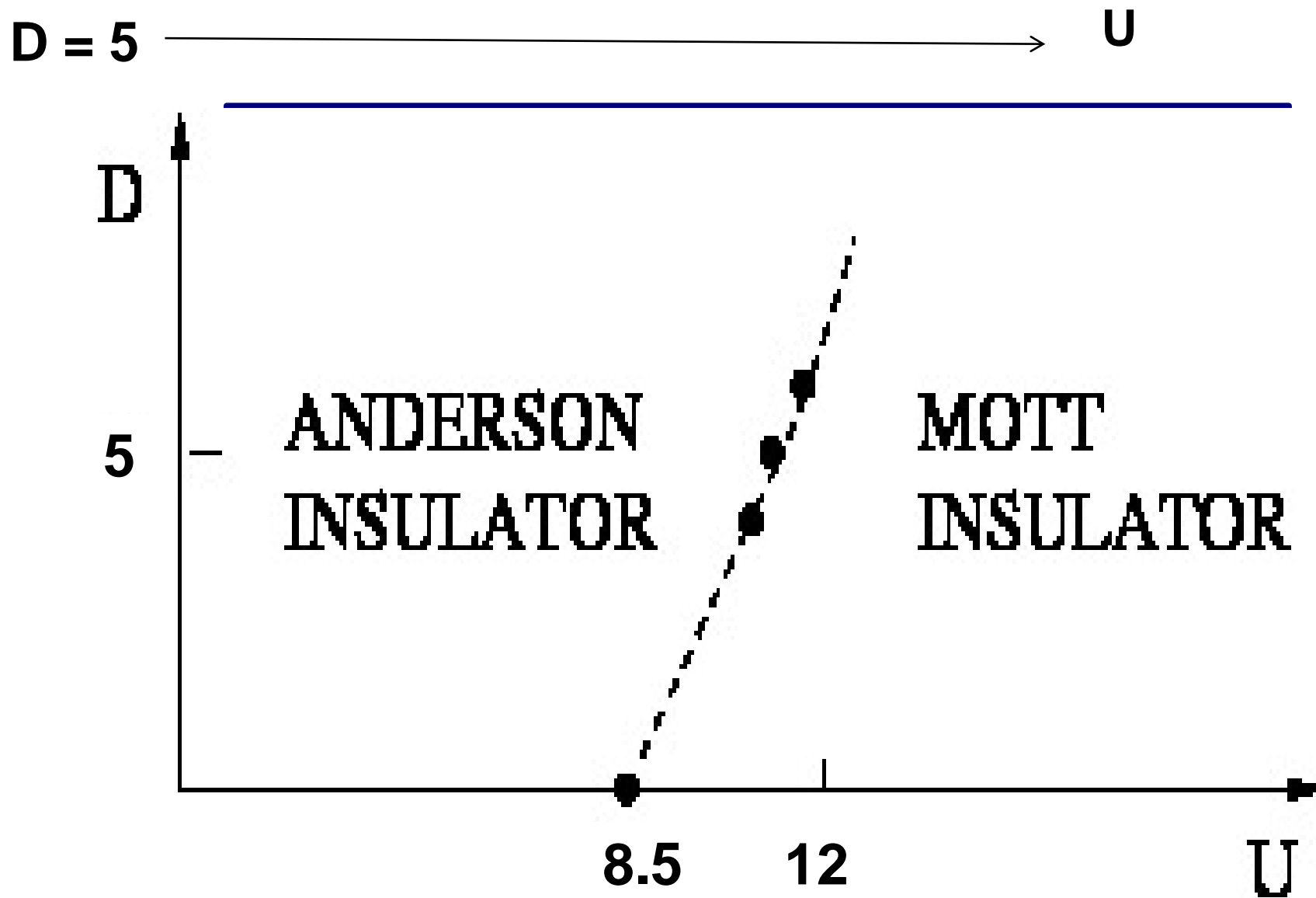


charge gap = 0 ANDERSON INSULATOR

charge gap 0 MOTT INSULATOR

Average energy of an excitation : (f-sum rule)

THE PARAMAGNETIC PHASE DIAGRAM



The Anderson-Mott transition

PARAMAGNETIC
ANDERSON INSULATOR

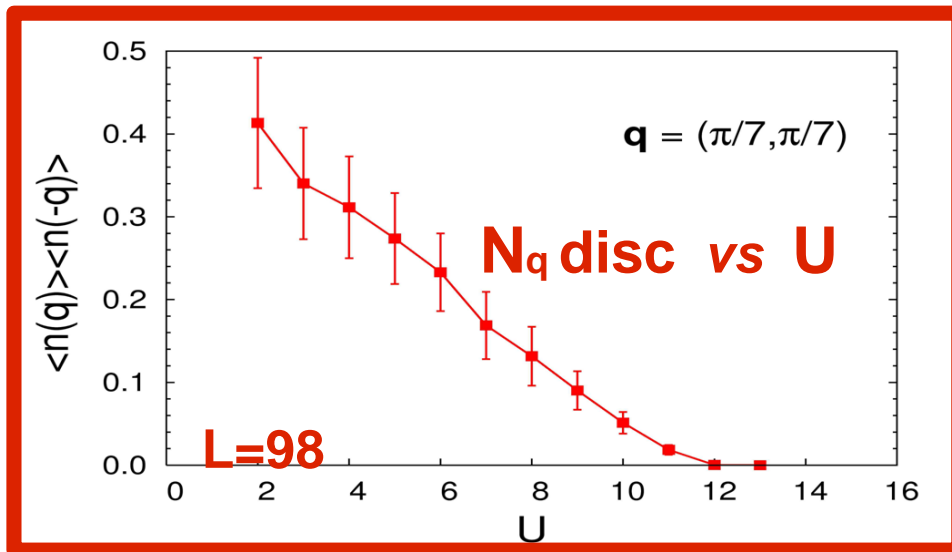
PARAMAGNETIC MOTT
INSULATOR

$U_c = 11.5 t$

U

What is the behaviour of N_q disconnected ?

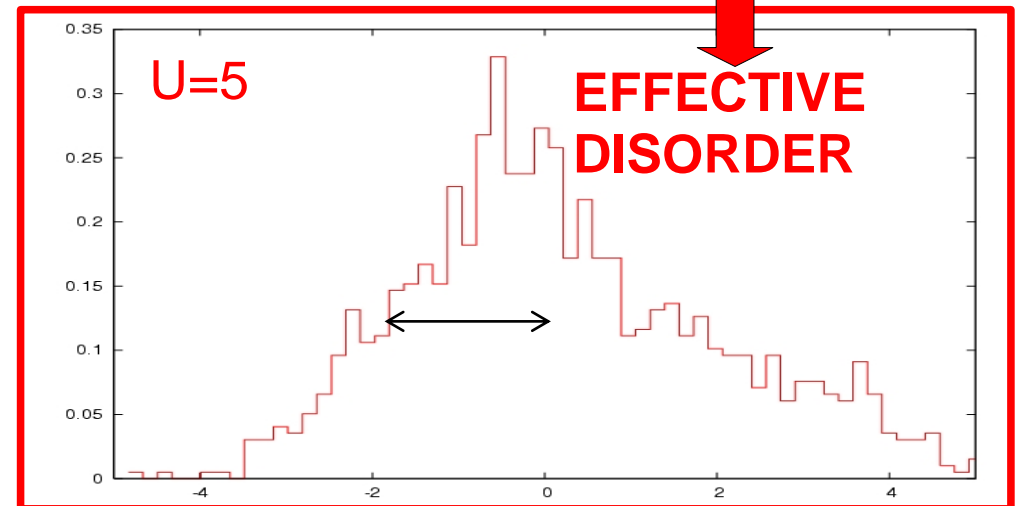
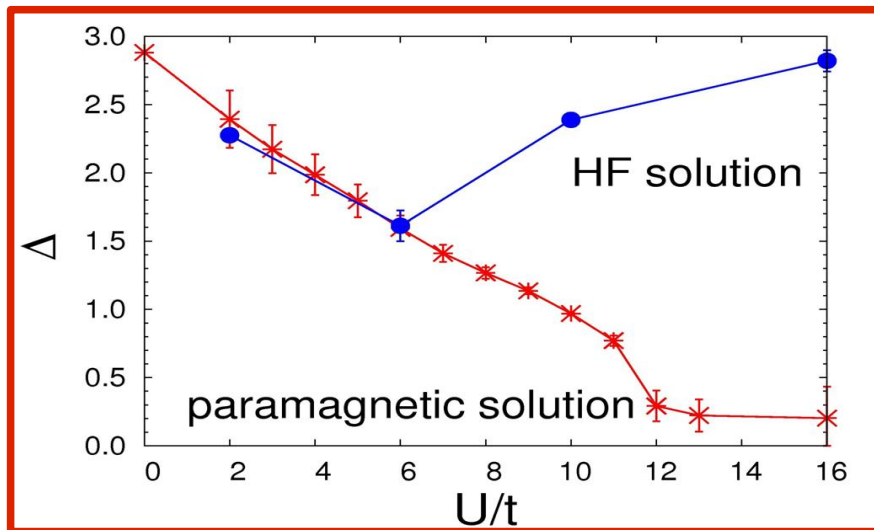
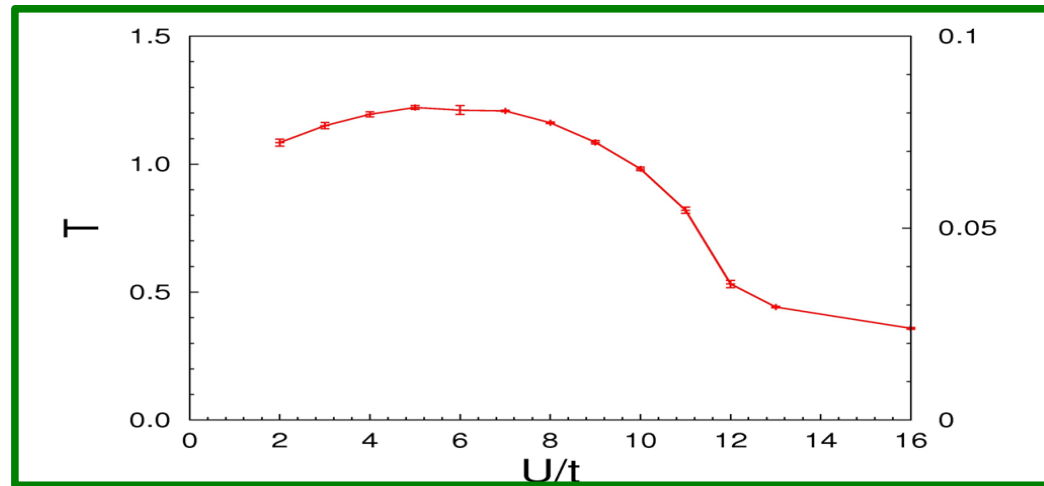
average over different
disorder realizations



**ORDER
PARAMETER !!**

compressibility fluctuations

INTERPLAY BETWEEN DISORDER AND INTERACTION (our results)

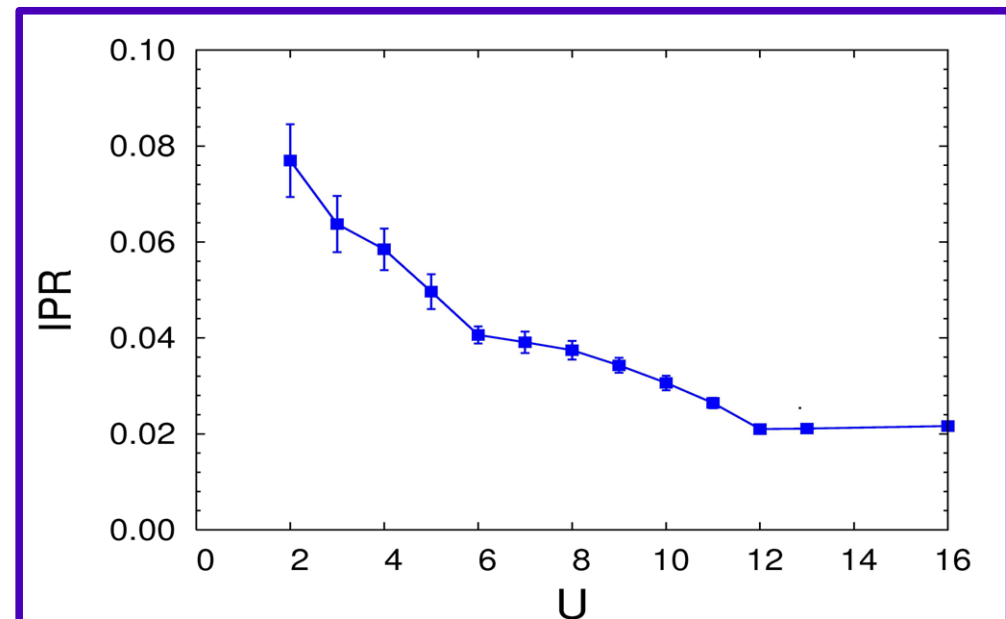


INTERPLAY BETWEEN DISORDER AND INTERACTION (our results)

Single particle wave function

COMPLETELY LOCALIZED STATE:

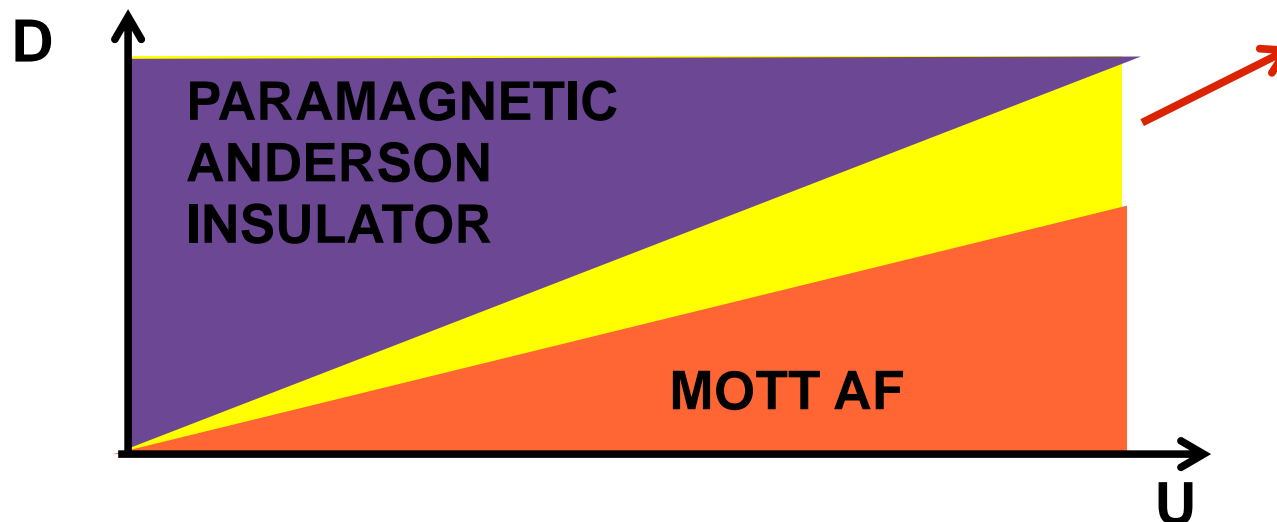
PLANE WAVE:



MAGNETIC PHASE DIAGRAM

ANDERSON INSULATOR

MOTT INSULATOR



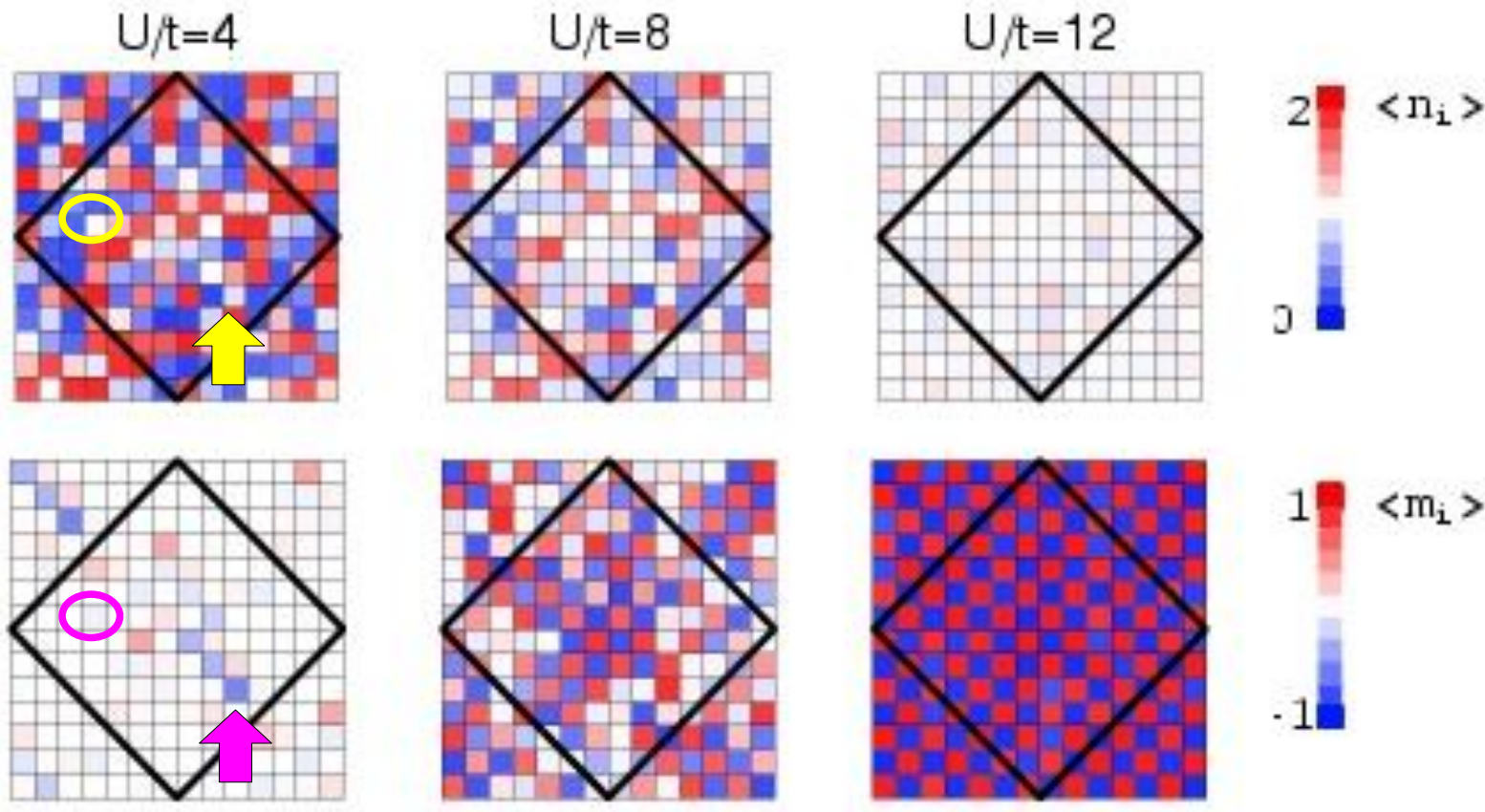
**INTERMEDIATE
PHASE**

localized states

gap = 0

AF order

LOCAL MAGNETIC MOMENTS



Presence of local magnetic moments at $T=0$

Local magnetic moments appear before the onset of long-range order: rare events

For a review on quantum Griffiths effects: Thomas Vojta arXiv: 1005.2707v1

EXPERIMENTS on (Si:P)

Paalanen et al., Phys. Rev. Lett. **57**, 2061
Hirsch et al., Phys. Rev. Lett. **68**, 1418

FURTHER DEVELOPMENTS

What (and how) can we say about the full many body wave Function ?

Is it localized or extended?

Local moments: are they dominating the thermodynamics of the system?

Thank you